Configuration and calibration of the BigBite spectrometer

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E05-102 Experimental Setup





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BigBite Spectrometer General Description

BigBite characteristics		
Configuration	Dipole	
Momentum range	$(200 - 900) \frac{\text{MeV}}{\text{c}}$	
Momentum acceptance	$-0.6 \leq \frac{\delta p}{p} \leq 0.8$	
Momentum resolution	4×10^{-3}	
Angular acceptance	100 msr	
Angular resolution	$\approx 1 \text{ mr}$	
Flight path (during $(e, e'd)$)	$\approx 3 \text{ m}$	
Maximum Field	$0.92 { m T}$	

BigBite Hadron detector package

- Two MWDCs for tracking, each consisting of 6 wire planes u,u',v,v',x,x'
- Two Scintillation planes E/dE for particle Identification & Energy determination



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The main purpose of the optics calibration is to determine the target variables $(y_{Tg}, \phi_{Tg}, \theta_{Tg}, \delta_{Tg})$ from the focal plane variables $(x_{Fp}, \theta_{Fp}, y_{Fp}, \phi_{Fp})$. There are many different ways to do that:

- Analytical Approximations
 - THaOpticsAnalytical, THaVertexTime Circular-arc approximation
 - THaOpticsAGen Effective-midplane approximation
- Transport matrix formalism
 - THaOpticsHRS

$$\begin{pmatrix} \delta_{Tg} \\ \theta_{Tg} \\ y_{Tg} \\ y_{Tg} \\ \phi_{Tg} \end{pmatrix} = \begin{pmatrix} \langle \delta_{Tg} | x_{Fp} \rangle & \langle \delta_{Tg} | \theta_{Fp} \rangle & \cdots & \cdots \\ \langle \theta_{Tg} | x_{Fp} \rangle & \langle \theta_{Tg} | \theta_{Fp} \rangle & \cdots & \cdots \\ \cdots & \cdots & \langle y_{Tg} | y_{Fp} \rangle & \langle y_{Tg} | \phi_{Fp} \rangle \\ \cdots & \cdots & \langle \phi_{Tg} | y_{Fp} \rangle & \langle \phi_{Tg} | \phi_{Fp} \rangle \end{pmatrix} \begin{pmatrix} x_{Fp} \\ \theta_{Fp} \\ y_{Fp} \\ \phi_{Fp} \end{pmatrix} + \cdots$$

Analytical Model THaVertexTime Quick Peek



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Transport Matrix Approach The Standard Approach

• Various parametrization of the matrix are possible. Here polynomial expansion is considered:

$$\Omega_{Tg} = \sum_{i,j,k} \theta_{Fp}^{i} y_{Fp}^{j} \phi_{Fp}^{k} \sum_{l=0}^{7} a_{ijkl}^{\Omega_{Tg}} x_{Fp}^{l}, \quad \Omega_{Tg} = (\delta_{Tg}, \theta_{Tg}, \phi_{Tg}, y_{Tg})$$

- Same matrix form as for the High Resolution Spectrometers. Ability to use the same code.
- Seasy to calculate with.
- Higher-order terms can cause bogus oscillations of the target variables. High-order matrix terms must be well under control.
- Calibration might not work beyond the limits set by the calibration points. Wild oscillations possible.

Ambition to get as close as possible to BigBite resolution from NIKHEF.



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y_{Tg} Calibration

- Quasi-Elastic ¹²C runs used with no sieve-slit
- Only coincidence events considered

$\phi_{Tg} \& \theta_{Tg}$ Calibration

- Quasi-Elastic ¹²C data with sieve slit
- Hydrogen (deuteron) elastic data used for absolute calibration and offset correction

δ_{Tq} Calibration

- Calibration with Missing-Mass peak reconstruction using Quasi-Elastic ²H data.
- Calibration with q-vector reconstruction for elastic runs using elastic ¹H and ²H data with BigBite set to different momenta

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Chronology y_{Tg} reconstruction

Oth Step

 Analytical approach to get a rough estimate of matrix elements

1st Attempt

- Manual approach to determine low order matrix elements
- Not useful for final analysis
- Low order matrix elements are robust used to check more sophisticated methods

Final Approach

• Final determination of matrix elements for further physical analysis





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y_{Tg} reconstruction - Final Approach

- Up to 5^{th} order matrix elements are considered.
- Started with 70 matrix elements, ended with 25
- Relevant matrix elements chosen using a combination of a Monte Carlo simulation of BigBite optics and manual selection.
- The determined set of the matrix elements is not unique. Other combinations of matrix elements could be used.
- **⑤** For calculation of matrix elements a χ^2 -minimization was used

$$\chi^{2}\left(a_{i}^{Tg}\right) = \sqrt{\left(y_{\text{Tg}}^{\text{True}} - y_{\text{Tg}}^{\text{Optics}}\left(x_{Fp}, y_{Fp}, \theta_{Fp}, \phi_{Fp}; a_{i}^{y_{Tg}}\right)\right)^{2}}$$

Oue to the numerical complexity of the minimization it is not certain that the solution is unique.

Robustness of the method

The robustness of the method is tested by checking the convergence of the minimization for a large number of randomly chosen initial sets of parameters.



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y_{Tg} reconstruction - Final Approach: Results

• ${}^{12}C(e, e'p)$ run #3491 with 7-foil target: $\sigma_{TgY} \approx 0.96 \,\mathrm{cm}$



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$\theta_{\mathit{Tg}} \text{ and } \phi_{\mathit{Tg}}$ Calibration $_{\text{Results}}$

- $\bullet\,$ For calibration a $3.5\,\mathrm{cm}\text{-thick}$ sieve slit collimator was used
- Most of the holes visible, some are out of the acceptance (obstructed by target Helmholtz coils)





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- δ_{Tg} is being determined using elastic H_2 and quasi-elastic D_2 data, by minimization of the width of the missing-mass peak.
- Current missing-mass resolution : $\sigma_{\delta_{Tg}} \lesssim 6 \, \text{MeV}/\text{c}^2$.



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Conclusion and Outlook

Conclusions

- Analytical model not very promising.
- Transport matrix gives better results. High-order terms must be well under control.
- Prefer matrix with low-order terms.
- We already have good results. Hoping for even better ones.

To-Do

- Determine better matrix elements for ϕ_{Tg} and δ_{Tg} .
- Reduce number of matrix elements for ϕ_{Tq} from 69 to ≈ 30 .
- Try to reduce number of matrix elements for other variables.
- Do all the necessary tests and check robustness of the method.
- Maybe try to make analytical model work.

Thank You! The End

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• Good optics helps us distinguish between protons and deuterons.

 $^{2}H(e, e'p)$ Calibration run #2164, $E_{beam} = 2 \text{ GeV}$



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Deuteron Selection

• For the calibration 1^{st} - and 2^{nd} -pass H runs and 2^{nd} -pass ${}^{2}H$ runs at different $p_{central}^{BB}$ (0.37 GeV/c) and 0.5 GeV/c) were used. For these runs $\vec{q} = \vec{p}_{proton}^{BB}$.

Problem

How to separate deuterons from protons in ${}^{2}H$ runs?

• Cuts on the dE/E plots: Calculating distance from the main band and selecting the events on the positive side.



y_{Tg} reconstruction - 1st Attempt

Matrix elements were determined by a semi-automatic method. Various scatter plots were used to determine how target variables depend on the focal-plane variables. Only two-variable dependencies were considered.

Step No.1

First determine how y_{Tg} depends on ϕ_{Fp} for different values of y_{Fp} . For each narrow cut on y_{Fp} we can find:

$$y_{Tg}(\phi_{Fp}) = c_1(y_{Fp})\phi_{Fp} + c_0(y_{Fp})$$

Step No.2

Determine how c_i depend on y_{Fp} :

$$c_i(y_{Fp}) = d_{i2}y_{Fp}^2 + d_{i1}y_{Fp} + d_{i3}$$

Results

Parameters d_{ij} are matrix elements for y_{Tg} .

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y_{Tg} reconstruction - 1st Attempt Demonstration





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$y_{\rm Tg}$ reconstruction - 1st Attempt: Results



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dE/E as alternative momentum reconstruction $_{\rm Background}$

• ADC signals from the dE and E planes can be used for particle ID as well as for the estimation of the particle momentum using the Bethe-Bloch equation:

$$\left(\frac{dE}{ds}\right)_{Bethe-Bloch} \propto \frac{Zz^2}{A} \rho \frac{1}{\beta^2} [1 + \cdots]$$

• Since plastic scintillators are used, Birks formula needs to be considered for the Light output of the scintillators:

$$\left(\frac{dL}{ds}\right)_{Mean} = A \frac{\left(\frac{dE}{ds}\right)}{1 + k_{Birks} \left(\frac{dE}{ds}\right)}$$

 Adjusting A_{dE}, A_E and k_{Birks} we can fit a theoretical curve to our data. In this way we can estimate the momentum of the events at different regions of the dE/E plots.

Exact calculations of momenta is impossible due to straggling, path-length distribution, etc.

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dE/E as alternative momentum reconstruction ${\rm A~good~example}$

• Elastic Hydrogen run #3488 at $E_b = 2 \text{ GeV}$, $p_p \approx 450 \frac{\text{MeV}}{c}$:



As a rough approximation,the method works reasonably well for this example: $\frac{\vec{p}-\vec{q}}{q} \approx +7\%$, $\sigma_{\vec{p}-\vec{q}} \approx 19 \frac{\text{MeV}}{\text{c}}$

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dE/E as alternative momentum reconstruction $\rm A \ bad \ example$

• Elastic Hydrogen run #1518 at $E_b = 1 \text{ GeV}, p_p \approx 340 \frac{\text{MeV}}{c}$:



Problem

Near the punch-through point all points correspond to the same mean energy-loss i.e. to the same momentum. Consequently an artificial sharp peak appears at the P.T.P.

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